

The group G is isomorphic to the group labelled by [1512, 779] in the Small Groups library.

Ordinary character table of $G \cong \text{PSL}(2,8) : \text{C3}$:

	1a	2a	3a	7a	9a	3b	3c	6a	6b	9b	9c
χ_1	1	1	1	1	1	1	1	1	1	1	1
χ_2	1	1	1	1	1	$E(3)$	$E(3)^2$	$E(3)$	$E(3)^2$	$E(3)$	$E(3)^2$
χ_3	1	1	1	1	1	$E(3)^2$	$E(3)$	$E(3)^2$	$E(3)$	$E(3)^2$	$E(3)$
χ_4	7	-1	-2	0	1	1	1	-1	-1	1	1
χ_5	7	-1	-2	0	1	$E(3)$	$E(3)^2$	$-E(3)$	$-E(3)^2$	$E(3)$	$E(3)^2$
χ_6	7	-1	-2	0	1	$E(3)^2$	$E(3)$	$-E(3)^2$	$-E(3)$	$E(3)^2$	$E(3)$
χ_7	21	-3	3	0	0	0	0	0	0	0	0
χ_8	8	0	-1	1	-1	2	2	0	0	-1	-1
χ_9	8	0	-1	1	-1	$2 * E(3)$	$2 * E(3)^2$	0	0	$-E(3)$	$-E(3)^2$
χ_{10}	8	0	-1	1	-1	$2 * E(3)^2$	$2 * E(3)$	0	0	$-E(3)^2$	$-E(3)$
χ_{11}	27	3	0	-1	0	0	0	0	0	0	0

Trivial source character table of $G \cong \text{PSL}(2,8) : \text{C3}$ at $p = 3$:

Normalisers N_i	N_1		N_2		N_3		N_4		N_5		N_6		N_7	
p -subgroups of G up to conjugacy in G	P_1		P_2		P_3		P_4		P_5		P_6		P_7	
Representatives $n_j \in N_i$	1a	2a	7a	1a	2a	1a	2a	1a	2a	1a	1a	2a	1a	2a
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 1 \cdot \chi_9 + 1 \cdot \chi_{10} + 0 \cdot \chi_{11}$	27	3	6	0	0	0	0	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 3 \cdot \chi_7 + 1 \cdot \chi_8 + 1 \cdot \chi_9 + 1 \cdot \chi_{10} + 0 \cdot \chi_{11}$	108	-12	3	0	0	0	0	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 1 \cdot \chi_{11}$	27	3	-1	0	0	0	0	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	36	-4	1	3	-1	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	9	1	2	3	1	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 3 \cdot \chi_7 + 1 \cdot \chi_8 + 1 \cdot \chi_9 + 1 \cdot \chi_{10} + 0 \cdot \chi_{11}$	90	-6	6	0	0	9	3	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 3 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	63	-9	0	0	0	9	-3	0	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 2 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	57	-7	1	3	-1	3	-1	3	-1	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	30	-2	2	3	1	3	1	3	1	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 3 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9 + 1 \cdot \chi_{10} + 0 \cdot \chi_{11}$	87	-9	3	0	0	6	0	0	0	3	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	3	3	3	0	0	3	3	0	0	0	3	3	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 3 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	84	-12	0	0	0	3	-3	0	0	0	3	-3	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	1	1	1	1	1	1	1	1	1	1	1	1	1	1
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	28	-4	0	1	-1	1	-1	1	-1	1	1	-1	1	-1

$$P_1 = \text{Group}([()]) \cong 1$$

$$P_2 = \text{Group}([(1, 5, 9)(6, 7, 8)]) \cong \text{C3}$$

$$P_3 = \text{Group}([(1, 9, 5)(2, 4, 3)(6, 7, 8)]) \cong \text{C3}$$

$$P_4 = \text{Group}([(1, 5, 9)(2, 4, 3), (1, 5, 9)(6, 7, 8)]) \cong \text{C3} \times \text{C3}$$

$$P_5 = \text{Group}([(1, 7, 4, 5, 6, 2, 9, 8, 3), (1, 5, 9)(2, 3, 4)(6, 8, 7)]) \cong \text{C9}$$

$$P_6 = \text{Group}([(1, 8, 3, 5, 7, 4, 9, 6, 2), (1, 5, 9)(2, 3, 4)(6, 8, 7)]) \cong \text{C9}$$

$$P_7 = \text{Group}([(1, 5, 9)(2, 4, 3), (1, 5, 9)(6, 7, 8), (1, 7, 4, 5, 6, 2, 9, 8, 3)]) \cong \text{C9} : \text{C3}$$

$$N_1 = \text{Group}([(1, 2)(3, 5)(4, 6)(7, 9), (2, 3, 4)(6, 7, 8)]) \cong \text{PSL}(2,8) : \text{C3}$$

$$N_2 = \text{Group}([(1, 5, 9)(6, 7, 8), (2, 3, 4)(6, 7, 8), (1, 6)(3, 4)(5, 7)(8, 9)]) \cong \text{C3} \times \text{S3}$$

$$N_3 = \text{Group}([(1, 9, 5)(2, 4, 3)(6, 7, 8), (2, 3, 4)(6, 7, 8), (2, 8)(3, 6)(4, 7)(5, 9), (1, 2, 6, 9, 4, 7, 5, 3, 8)]) \cong \text{C9} : \text{C6}$$

$$N_4 = \text{Group}([(2, 3, 4)(6, 7, 8), (1, 5, 9)(2, 4, 3), (2, 8)(3, 6)(4, 7)(5, 9), (1, 2, 6, 9, 4, 7, 5, 3, 8)]) \cong \text{C9} : \text{C6}$$

$$N_5 = \text{Group}([(1, 7, 4, 5, 6, 2, 9, 8, 3), (1, 5, 9)(2, 3, 4)(6, 8, 7), (2, 4, 3)(6, 8, 7)]) \cong \text{C9} : \text{C3}$$

$$N_6 = \text{Group}([(1, 8, 3, 5, 7, 4, 9, 6, 2), (1, 5, 9)(2, 3, 4)(6, 8, 7), (2, 3, 4)(6, 7, 8), (2, 6, 4, 8, 3, 7)(5, 9)]) \cong \text{C9} : \text{C6}$$

$$N_7 = \text{Group}([(1, 8, 2, 5, 7, 3, 9, 6, 4), (2, 4, 3)(6, 8, 7), (1, 5, 9)(2, 4, 3), (2, 8)(3, 6)(4, 7)(5, 9)]) \cong \text{C9} : \text{C6}$$